



# **Droplet moving over a sharp transition of wettability on the hydrophobic surface**

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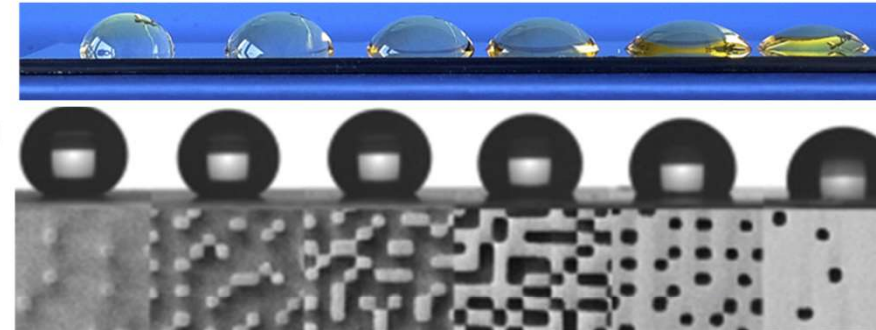


## Hydrophobic surface

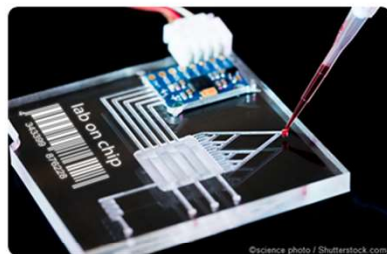


MacGregor-Ramiasa MN, Vasilev K. *Advanced Materials Interfaces*. 2017 Aug;4(16):1700381.

## Gradient: chemical(above) or roughness (below)



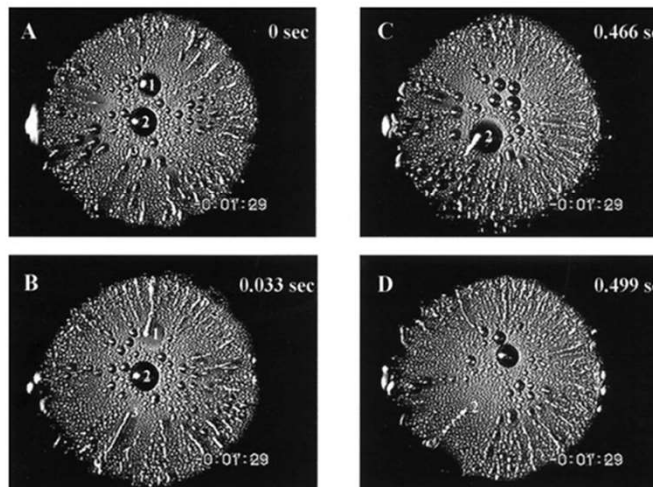
Gradient  
Less hydrophobic →



## microfluidic system

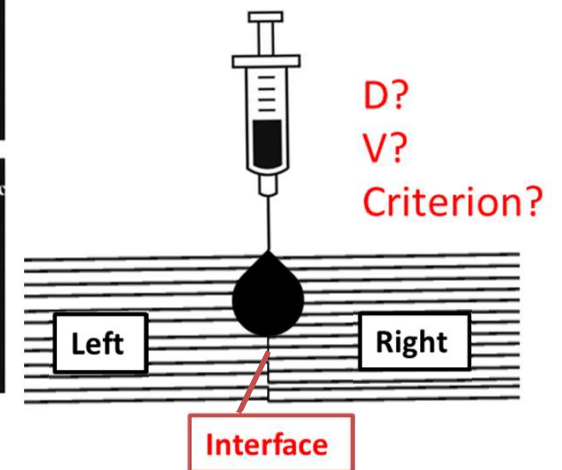
Accuracy  
Avoid Interference

Drop-wise  
Efficiency



## Heat transfer enhancement

S. Daniel, *Science* (80-. ), 2001, 291, 633–636.





## Surface design

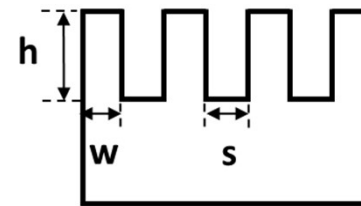
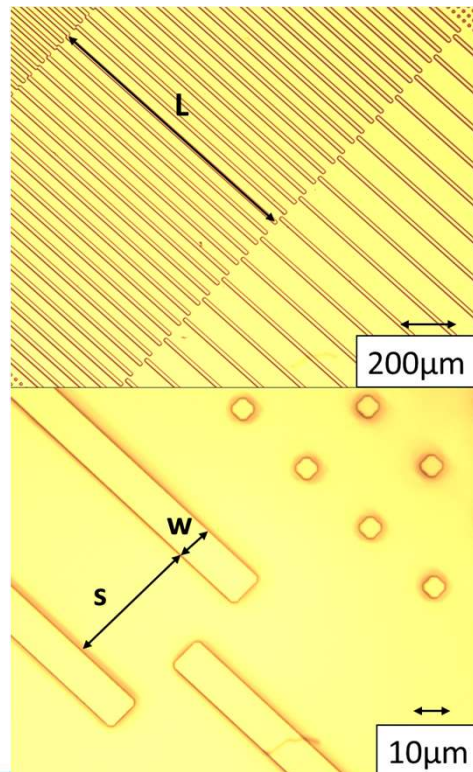
microstructure

Width: 10 μm

Spacing: 5-90 μm

Height: 20 μm

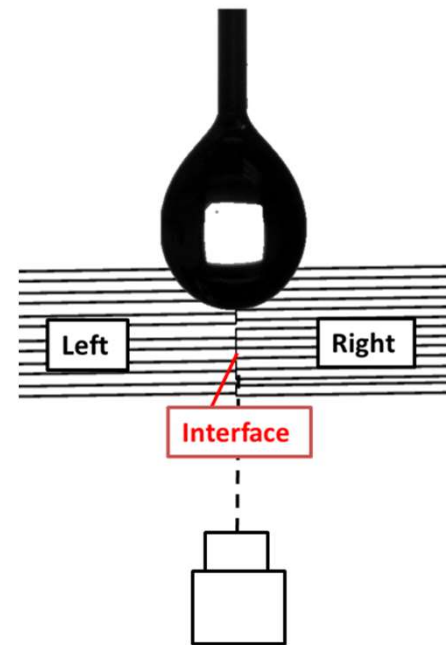
Contact Angle: 110-155°



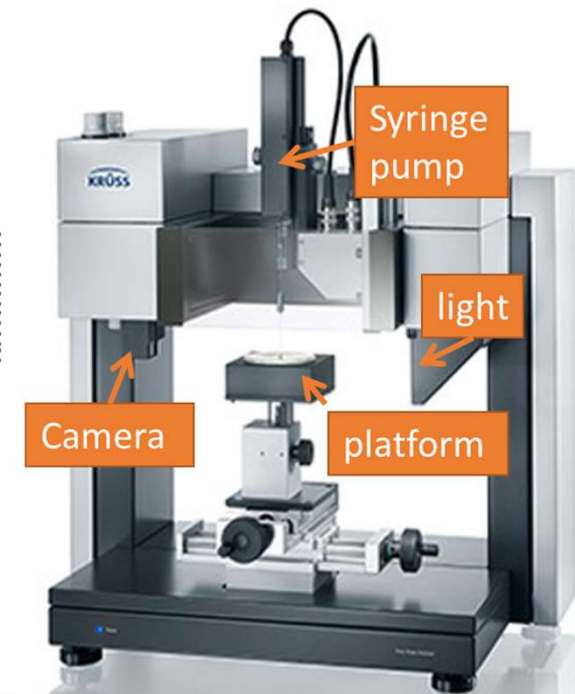
Left **Interface** Right

9 kinds of surface units

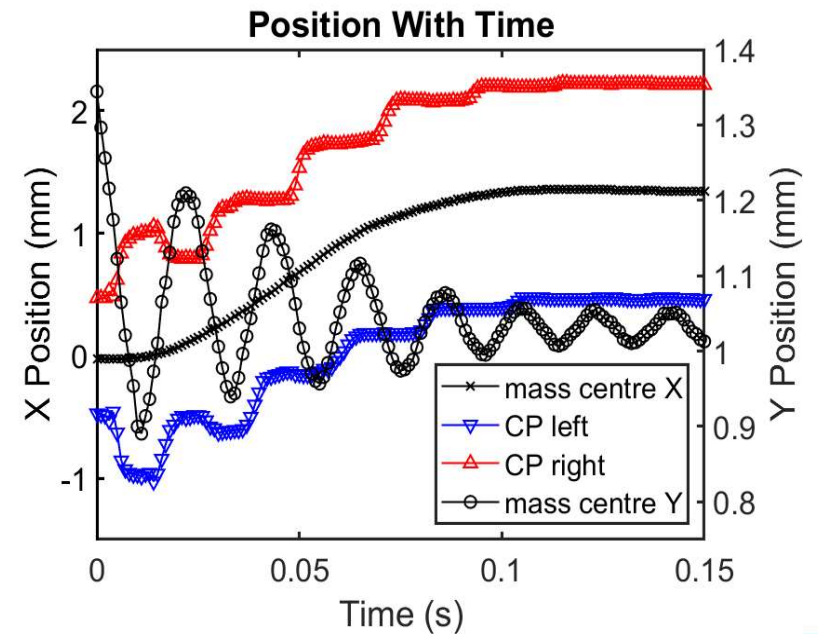
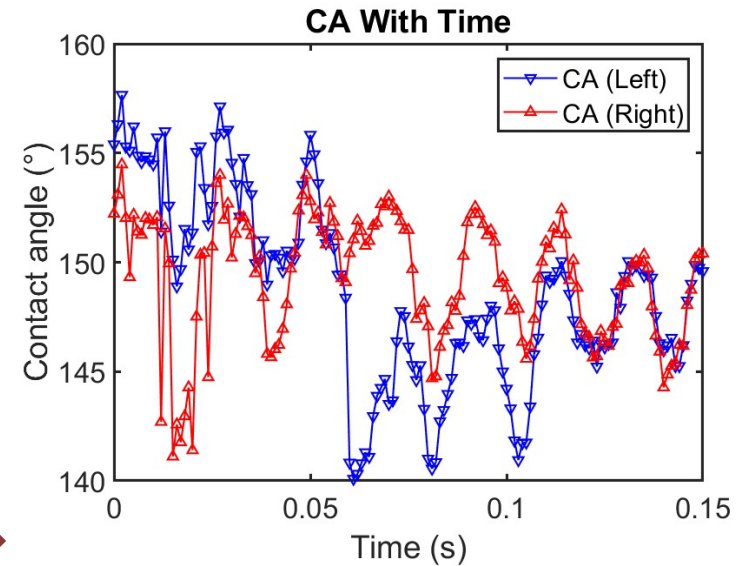
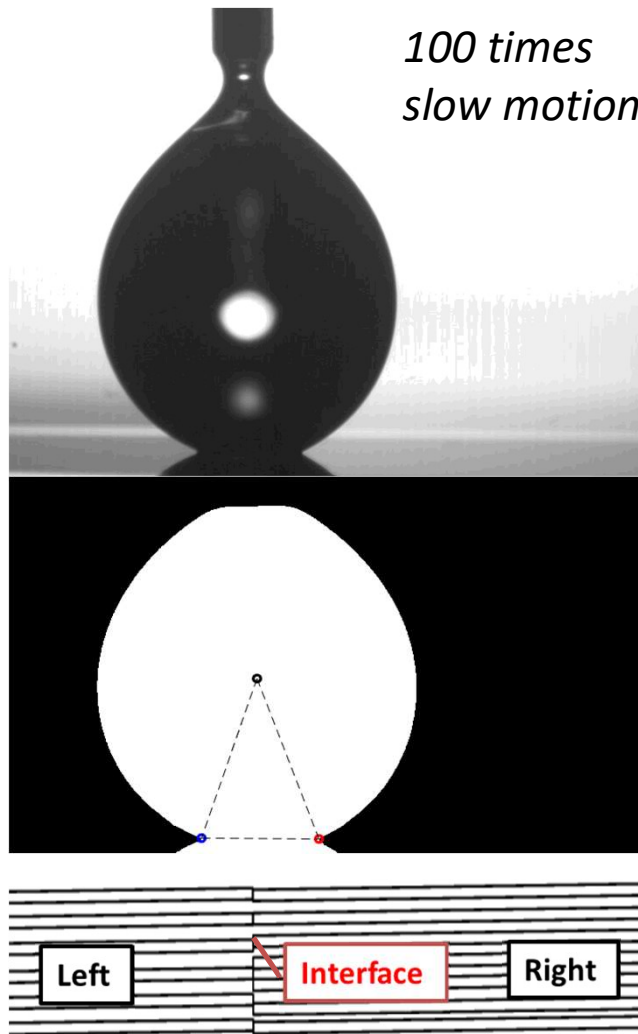
$$\frac{9 \cdot 8}{2} = 36 \text{ combinations}$$



High-speed Camera









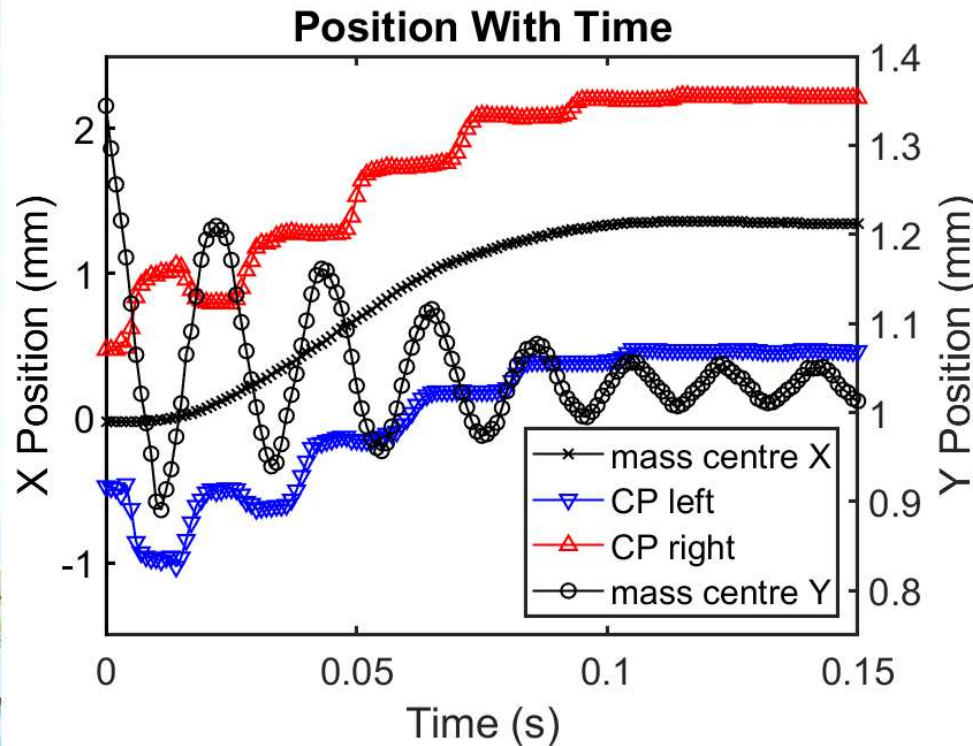
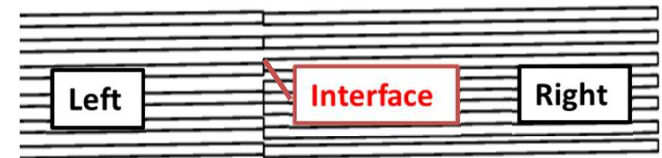
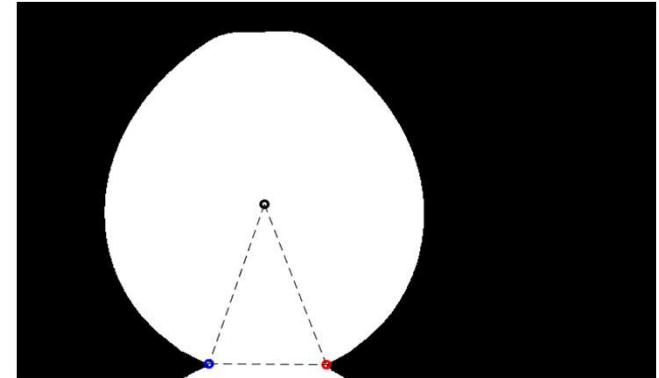
## Horizontal 'drift' — mass centre

Driving Force:  $F_d = \gamma R (\cos \theta_{eq}^R - \cos \theta_{eq}^L)$

Resistance:  $f_v \sim \beta V$

$f_f$

$f_h \sim \theta_{ad}^L, \theta_{re}^L, \theta_{ad}^R, \theta_{re}^R$



## Damped Oscillation

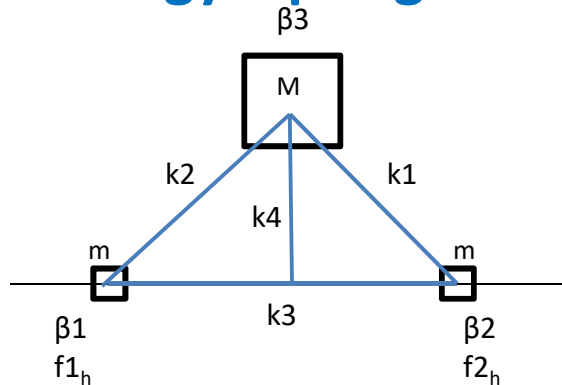
Motion activation

More than superposition

Drift  $\Leftrightarrow$  Oscillation

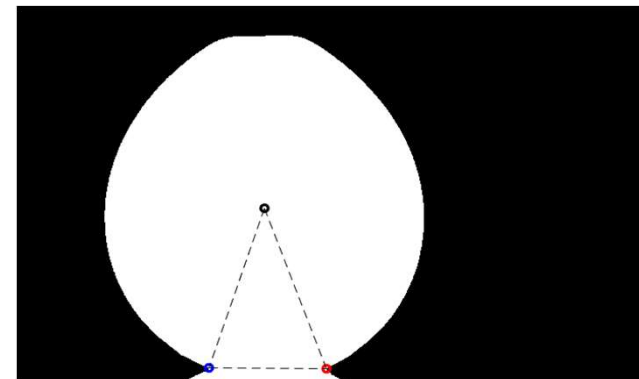


## Analogy: Spring model

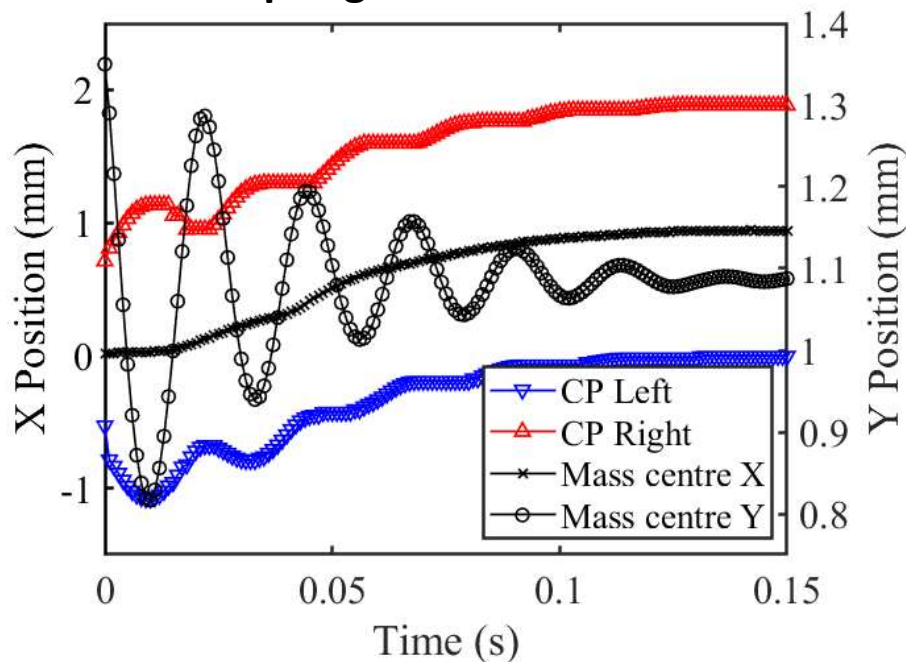


$$M \gg m$$

$$F_d, f_f, f_v, f_h$$

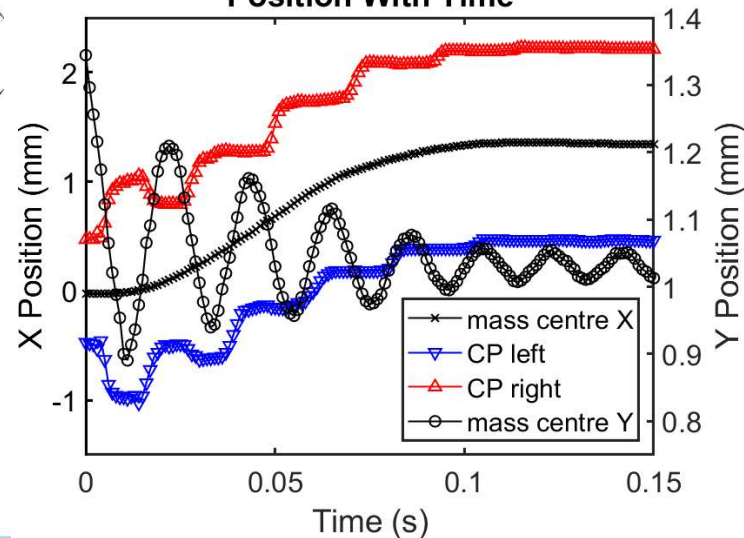


### Spring model result



### Experimental data

#### Position With Time



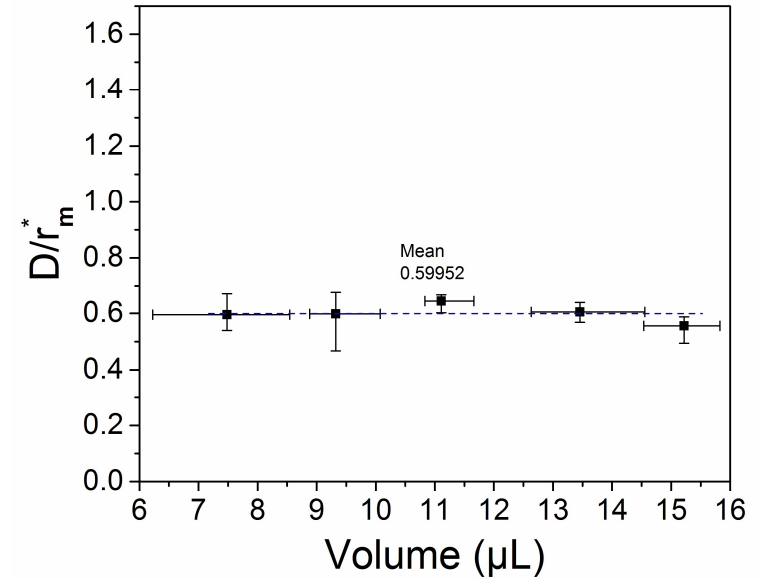


## Volume influence

Normalized displacement

$$r_{l,r}^* = \left(\frac{3V}{\pi}\right)^{1/3} (1 - \cos \theta_{eq}^{L,R})^{-2/3} (2 + \cos \theta_{eq}^{L,R})^{-1/3}$$

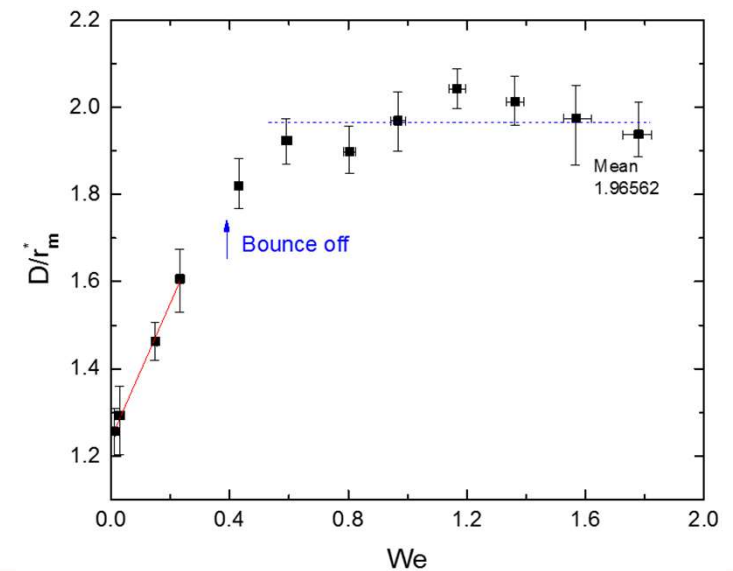
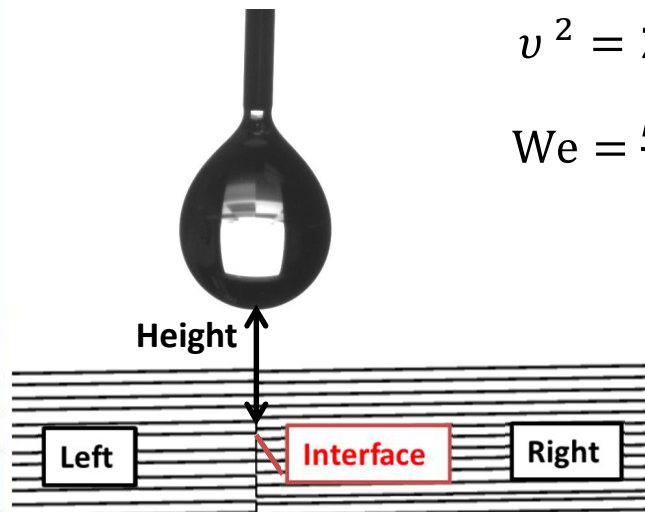
$$r_m^* = (r_l^* + r_r^*)/2$$



## Height influence

$$v^2 = 2gH$$

$$We = \frac{\rho v^2}{\gamma} = \frac{2gH}{\gamma}$$





## Overall cases: motion distance

$$\Delta\varphi = \varphi_R - \varphi_L$$

### Driving force

Caused by gradient

$$F_d = \gamma(\cos\theta_{eq}^R - \cos\theta_{eq}^L) \\ = \gamma(1 + \cos\theta_Y)\Delta\varphi$$

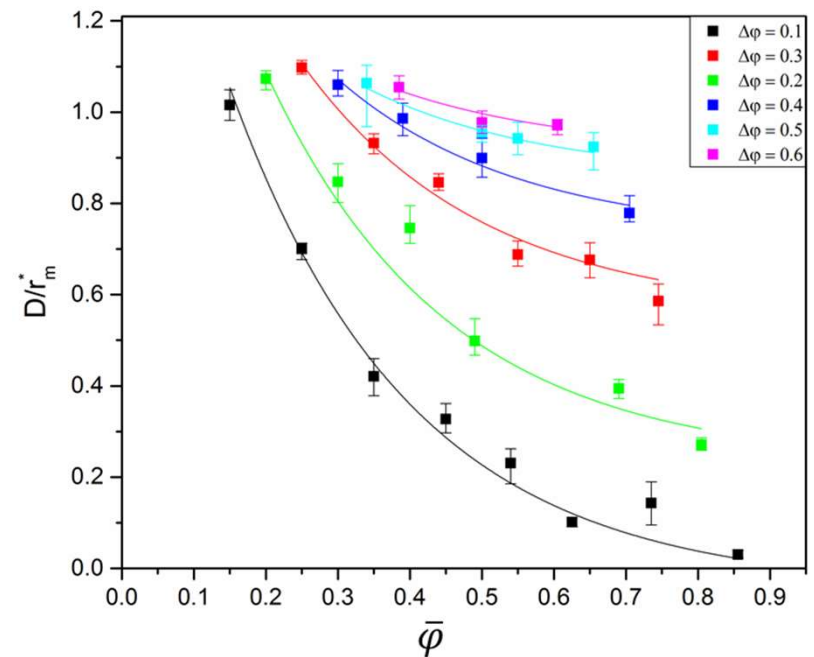
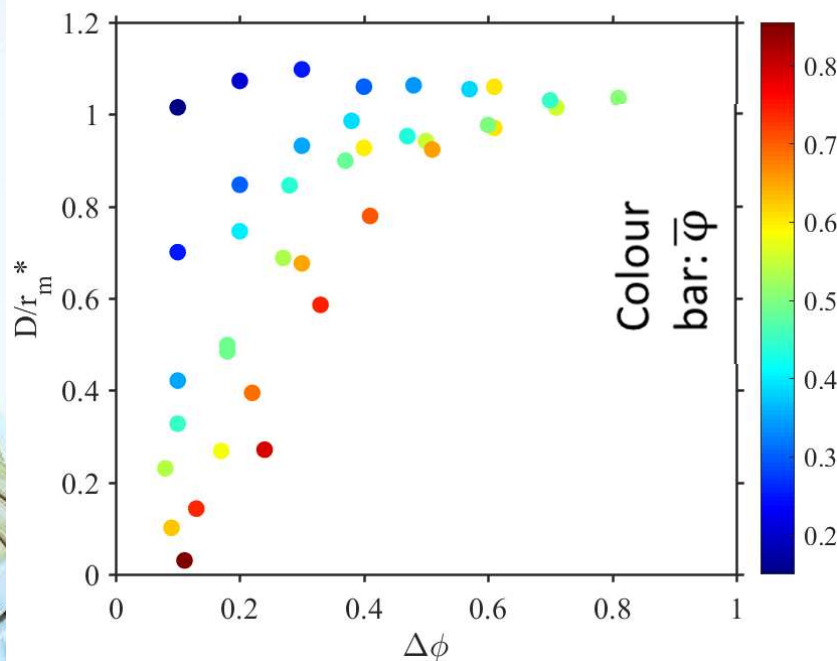
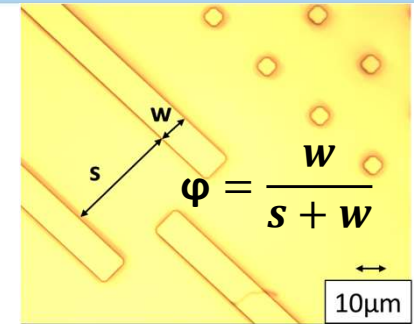
$$\bar{\varphi} = \frac{(\varphi_R + \varphi_L)}{2}$$

### Resistance

Friction and hysteresis

'sliding' and 'static' friction force

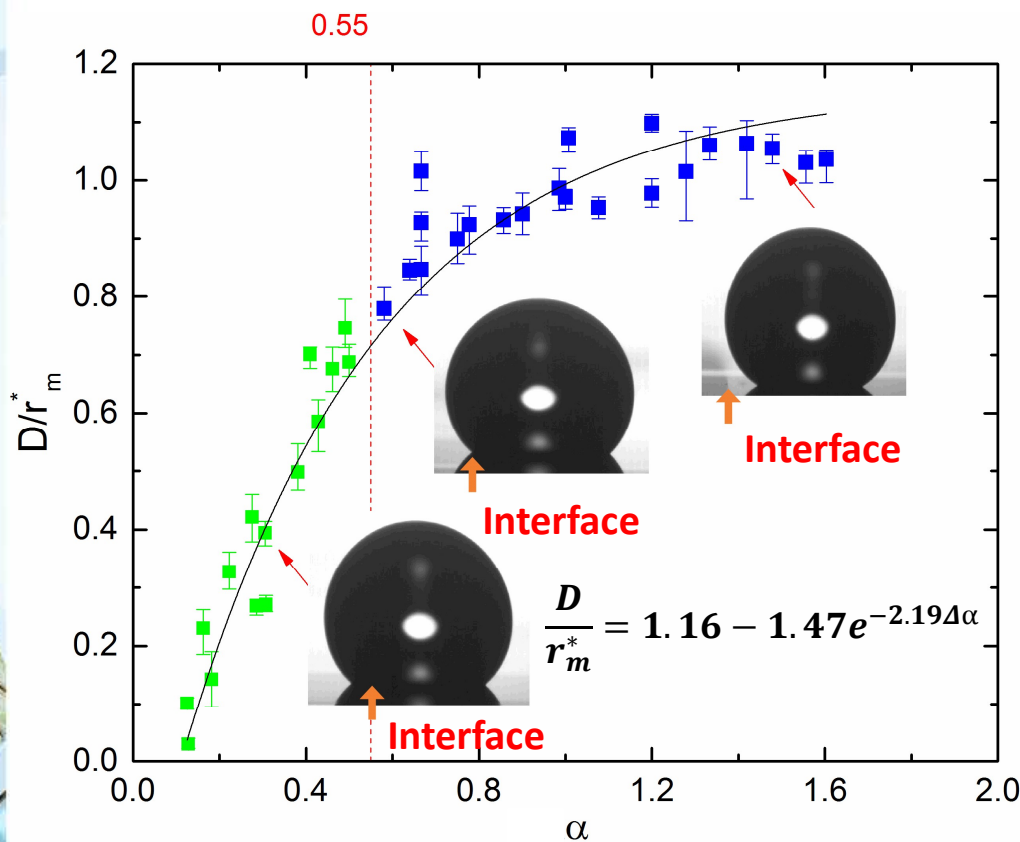
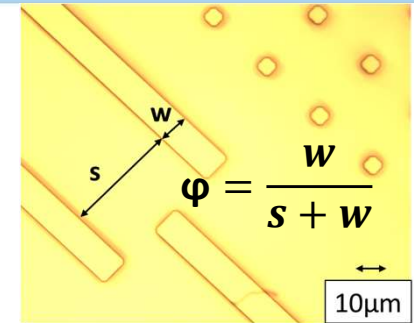
$$F_r: f_f, f_h \sim \bar{\varphi}$$





## Overall cases: motion distance

$$\alpha = \frac{2(\varphi_R - \varphi_L)}{\varphi_R + \varphi_L} = \frac{\Delta\varphi}{\bar{\varphi}} = \frac{F_d}{F_r}$$



### Driving force

$$F_d = \gamma(\cos \theta_R - \cos \theta_L) = \gamma(1 + \cos \theta_Y)\Delta\varphi$$

### Resistance

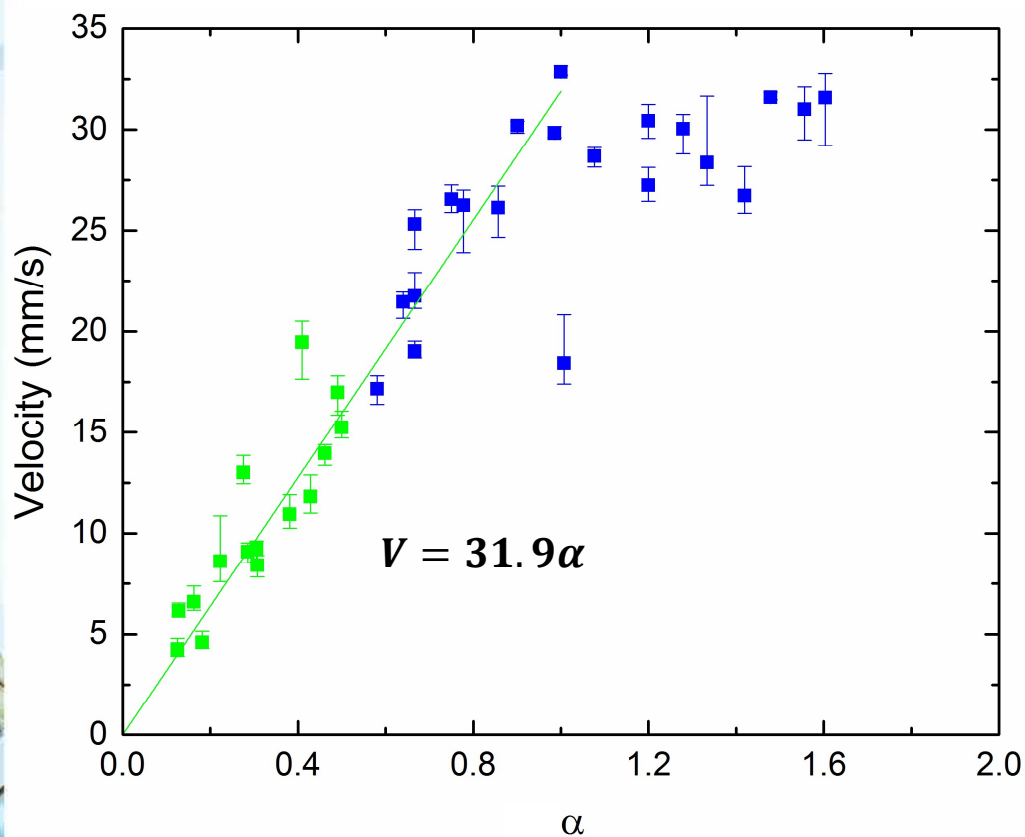
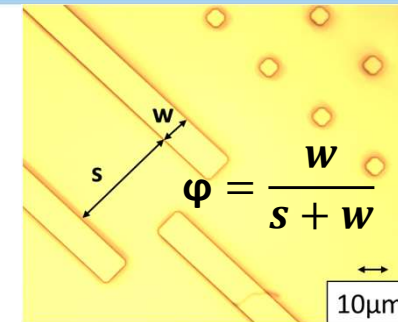
Friction and hysteresis

$$F_r \sim \bar{\varphi}$$

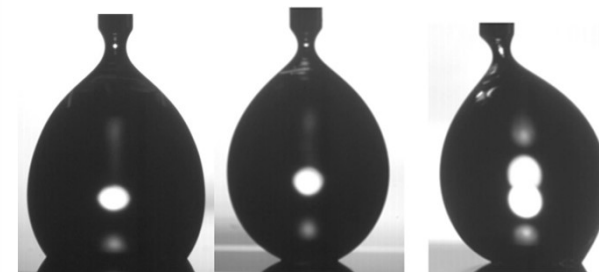


## Overall cases: Average Velocity

$$\alpha = \frac{2(\varphi_R - \varphi_L)}{\varphi_R + \varphi_L} = \frac{\Delta\varphi}{\bar{\varphi}} = \frac{F_d}{F_r}$$



## Initial deposition



$\alpha = 0.18$      $\alpha = 0.67$      $\alpha = 1.56$

Viscous force  $f_v$ ?

$$f_v \sim \beta V$$



## Single motion analysis:

Coupling of two motion behaviors

Analogy method: spring model

## Overall cases:

Volume has little influence

Increase with  $We$  at a small range

A criterion combining  $F_d$  and  $F_r$

Fundamental understanding

Beneficial for Microfluidic device design





**Thank you for your attention!**

